

Student: \_\_\_\_\_  
 Date: \_\_\_\_\_  
 Time: \_\_\_\_\_

Instructor: Lance Burger  
 Course: Fall 2015 Fresno State Math 75 -  
 Burger  
 Book: California State University, Fresno:  
 Math 75/76/77

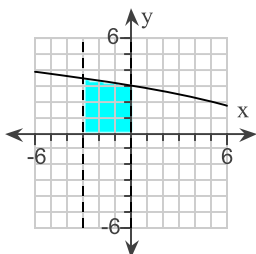
Assignment: 5.2

1. Use geometry (not Riemann sums) to evaluate the definite integral. Sketch the graph of the integrand, show the region in question, and interpret your result.

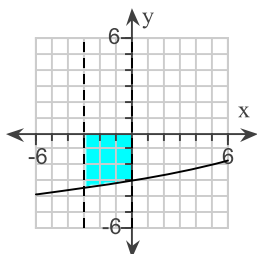
$$\int_{-3}^0 \sqrt{9-x^2} \, dx$$

Choose the correct graph below.

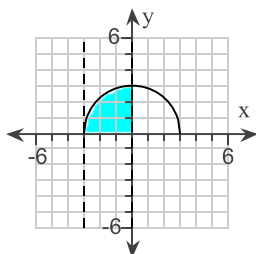
☐ A.



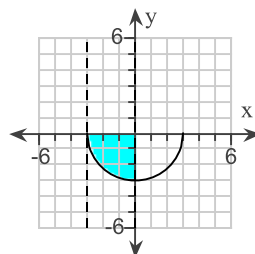
☐ B.



☐ C.



☐ D.



The value of the definite integral  $\int_{-3}^0 \sqrt{9-x^2} \, dx$  as determined by the area under the graph of the integrand is .

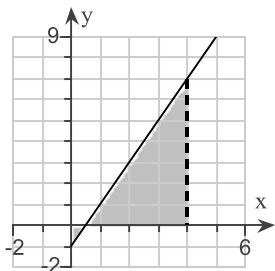
(Simplify your answer. Type an exact answer, using  $\pi$  as needed. Use integers or fractions for any numbers in the expression.)

2. Use geometry (not Riemann sums) to evaluate the following definite integral. Sketch a graph of the integrand, show the region in question, and interpret your results.

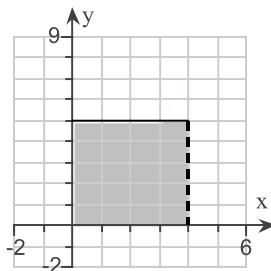
$$\int_0^4 f(x) \, dx \text{ where } f(x) = \begin{cases} 5 & \text{if } x \leq 3 \\ 2x - 1 & \text{if } x > 3 \end{cases}$$

Sketch a graph of the integrand, and then shade the region in question. Choose the correct graph below.

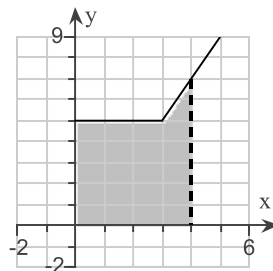
☐ A.



☐ B.



☐ C.



$\int_0^4 f(x) \, dx =$   (Simplify your answer. Type an integer or a decimal.)

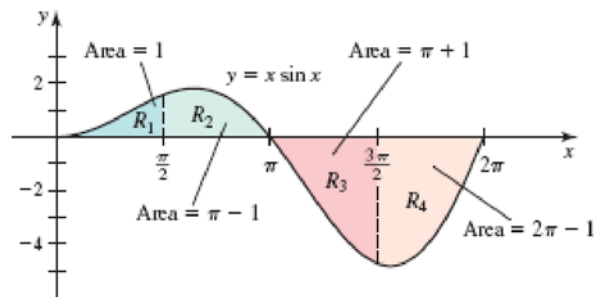
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3. The figure to the right shows four regions bounded by the graph of  $y = x \sin x$ :  $R_1$ ,  $R_2$ ,  $R_3$ , and  $R_4$ , whose areas are  $1$ ,  $\pi - 1$ ,  $\pi + 1$ , and  $2\pi - 1$ , respectively. Use this information to evaluate the following integral.

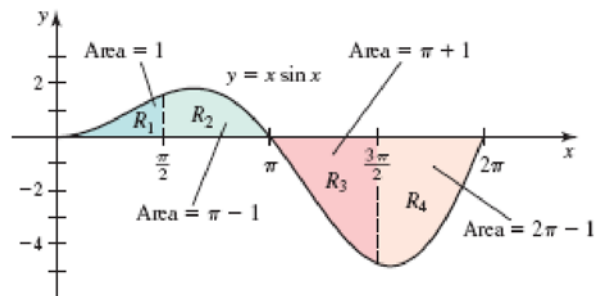
$$\int_0^{3\pi/2} x \sin x \, dx$$



$$\int_0^{3\pi/2} x \sin x \, dx = \boxed{\phantom{000}} \text{ (Type an exact answer, using } \pi \text{ as needed.)}$$

4. The figure to the right shows four regions bounded by the graph of  $y = x \sin x$ :  $R_1$ ,  $R_2$ ,  $R_3$ , and  $R_4$ , whose areas are  $1$ ,  $\pi - 1$ ,  $\pi + 1$ , and  $2\pi - 1$ , respectively. Use this information to evaluate the following integral.

$$\int_0^{\pi} x \sin x \, dx$$



$$\int_0^{\pi} x \sin x \, dx = \boxed{\phantom{000}} \text{ (Type an exact answer, using } \pi \text{ as needed.)}$$

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5. Use only the fact that  $\int_5^6 6x(8-x)dx = 82$  and the definitions and properties of integrals to evaluate the integrals in parts a through d, if possible.

a. Choose the correct answer below and, if necessary, fill in the answer box to complete your choice.

- ☐ A.  $\int_6^5 6x(8-x)dx = \square$   
(Simplify your answer. Type an exact answer, using radicals as needed.)
- ☐ B. The integral cannot be calculated.

b. Choose the correct answer below and, if necessary, fill in the answer box to complete your choice.

- ☐ A.  $\int_5^6 x(8-x)dx = \square$   
(Simplify your answer. Type an exact answer, using radicals as needed.)
- ☐ B. The integral cannot be calculated.

c. Choose the correct answer below and, if necessary, fill in the answer box to complete your choice.

- ☐ A.  $\int_6^5 30x(8-x)dx = \square$   
(Simplify your answer. Type an exact answer, using radicals as needed.)
- ☐ B. The integral cannot be calculated.

d. Choose the correct answer below and, if necessary, fill in the answer box to complete your choice.

- ☐ A.  $\int_5^{12} 6x(8-x)dx = \square$   
(Simplify your answer. Type an exact answer, using radicals as needed.)
- ☐ B. The integral cannot be calculated.

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6. Suppose  $\int_2^4 f(x) dx = 3$ ,  $\int_2^7 f(x) dx = -3$ , and  $\int_2^7 g(x) dx = -7$ . Evaluate the following integrals.

$$\int_7^2 g(x) dx = \square$$

(Simplify your answer.)

$$\int_2^7 2g(x) dx = \square$$

(Simplify your answer.)

$$\int_2^7 [g(x) - f(x)] dx = \square$$

(Simplify your answer.)

$$\int_2^7 [4g(x) - f(x)] dx = \square$$

(Simplify your answer.)

7. Use the value of the first integral I to evaluate the two given integrals.

$$I = \int_0^1 (x^3 - 3x) dx = -\frac{5}{4}$$

a.  $\int_0^1 (6x - 2x^3) dx$

b.  $\int_1^0 (3x - x^3) dx$

a.  $\int_0^1 (6x - 2x^3) dx = \square$  (Simplify your answer.)

b.  $\int_1^0 (3x - x^3) dx = \square$  (Simplify your answer.)

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1.  $C$   
 $\frac{9\pi}{4}$

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2.  $C$   
21

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3.  $-1$

---

4.  $\pi$

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5. A,  $-82$   
A,  $\frac{41}{3}$   
A,  $-410$   
B

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6. 7  
 $-14$   
 $-4$   
 $-25$

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7.  $\frac{5}{2}$   
 $-\frac{5}{4}$

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